

Show all work clearly. Circle your final answers. Simplify as much as possible.

**1.** The position  $y$  (in feet) of a particle at time  $t$  (in seconds) is given by the formula

$$y = t^3 - 3t + 4.$$

(a) Find the average speed of the particle between  $t = 1$  and  $t = 2$  seconds. Be sure to include appropriate units.

(b) Find and simplify a formula for the average speed of the particle on the time interval  $[1, 1 + h]$ ,  $h \neq 0$ . Leave your answer in terms of  $h$ .

(c) Use your formula from part (b) to compute the average speed of the particle on the time intervals  $[1, 1.1]$ , and  $[1, 1.01]$ , and  $[1, 1.001]$ . Round your answers to at least 3 decimal places.

(d) Using your data from part (c), what seems to be the instantaneous speed of the particle at time  $t = 1$  second?

**2.** Sketch a graph of each of the following functions and explain why the limit does not exist.

(a)  $f(x) = \frac{x}{|x|}$ ;  $\lim_{x \rightarrow 0} f(x)$

(b)  $g(x) = \frac{1}{x-1}$ ;  $\lim_{x \rightarrow 1} g(x)$

**3.** Find and simplify the difference quotient  $\frac{f(x+h) - f(x)}{h}$ ,  $h \neq 0$  for the function  $f(x) = \frac{1}{x}$ . What happens to the difference quotient as  $h \rightarrow 0$ ?

**4.** Evaluate the following limits.

(a)  $\lim_{x \rightarrow -1} \frac{x^3 + 3x + 2}{x^2 - x - 2}$

(b)  $\lim_{x \rightarrow -1} \frac{\sqrt{x^2 + 8} - 3}{x + 1}$  (Hint: Rationalize the numerator.)

**5.** Use the Sandwich Theorem to show that  $\lim_{x \rightarrow 0} x^2 \cos(20\pi x) = 0$ . (Hint: Find two functions  $f$  and  $g$  with  $f(x) \leq x^2 \cos(20\pi x) \leq g(x)$  and  $\lim_{x \rightarrow 0} f(x) = \lim_{x \rightarrow 0} g(x) = 0$ .)