
Math 110 Supplemental Instruction Worksheet 6

1. Hot Topic is running a special: for \$5, you choose a paper bag from a bin which contains a mystery t-shirt. Suppose the bin contains 20 t-shirts, each with a different design. You only like 12 of their 20 t-shirt designs, but you buy five of them anyway.

(a) What is the probability that you like all five shirts that you bought?

$$P(\text{like all five}) = \frac{\# \text{ buy five \& like}}{\# \text{ buy five}} = \frac{792}{15504} = \frac{33}{646}$$

#ways to buy five & like:

$$C(12, 5) = \frac{12!}{7!5!} = 792$$

#ways to buy five:

$$C(20, 5) = \frac{20!}{15!5!} = 15504$$

(b) What is the probability that you like at least two of the shirts that you bought?

options: like 2, dislike 3 $P(\text{like at least two}) = \frac{\# \text{ ways to like at least 2 of 5}}{\# \text{ ways to buy 5}}$

like 3, dislike 2

like 4, dislike 1

like 5, dislike 0

$$= \frac{14608}{15504} = \frac{913}{969}$$

#ways to like at least 2:

$$\begin{aligned} & C(12, 2) \cdot C(8, 3) = 66 \cdot 56 \\ + & C(12, 3) \cdot C(8, 2) = 220 \cdot 28 \\ + & C(12, 4) \cdot C(8, 1) = 495 \cdot 8 \\ + & C(12, 5) = 792 \\ \hline & 14608. \end{aligned}$$

OR $P(\text{like at least two}) = 1 - P(\text{like 0 or 1})$

2. You pick four stones out of a bag consisting of 4 diamonds and 16 diamond shaped pieces of glass.

(a) What is the probability that you did not get any diamonds?

$$P(\text{no diamonds}) = \frac{\# \text{ ways to get 4 glass}}{\# \text{ ways to get 4}} = \frac{1820}{4845} = \frac{364}{969}$$

4 glass:

$$C(16, 4) = 1820$$

Any 4:

$$C(20, 4) = 4845$$

(b) What is the probability that you got at least one diamond?

$$P(\text{at least one diamond}) = 1 - P(\text{no diamond})$$
$$= 1 - \frac{364}{969} = \frac{605}{969}$$

3. A baseball team has 12 pitchers, 7 infielders and 6 outfielders. Suppose three players are picked at random to be team captains. Find the probability:

(a) All three captains are pitchers.

$$P(3 \text{ pitchers}) = \frac{\# \text{ ways to select 3 pitchers}}{\# \text{ ways to select 3 players}} = \frac{C(12,3)}{C(25,3)}$$
$$= \frac{220}{2300} = \frac{11}{115}$$

(b) There is one pitcher, one infielder and one outfielder.

$$P(\text{one each}) = \frac{\# \text{ ways to pick one each}}{\# \text{ ways to pick 3 players}} = \frac{C(12,1) \cdot C(7,1) \cdot C(6,1)}{C(25,3)}$$
$$= \frac{504}{2300} = \frac{126}{575}$$

(c) There is no outfielder picked as a captain.

$$P(\text{no outfielder}) = \frac{\# \text{ ways to pick pitcher \& mf only}}{\# \text{ ways to pick any 3}}$$
$$= \frac{C(19,3)}{C(25,3)} = \frac{969}{2300}$$